

**AQA Computer Science A-Level**  
**4.3.4 Searching algorithms**  
Advanced Notes



## **Specification:**

### **4.3.4.1 Linear search:**

Know and be able to trace and analyse the complexity of the linear search algorithm. Time complexity is  $O(n)$ .

### **4.3.4.2 Binary search**

Know and be able to trace and analyse the time complexity of the binary search algorithm. Time complexity is  $O(\log n)$ .

### **4.3.4.3 Binary tree search**

Be able to trace and analyse the time complexity of the binary tree search algorithm. Time complexity is  $O(\log n)$ .



## Searching Algorithms

An **algorithm** is a set of **instructions** which completes a **task** in a **finite time** and always **terminates**. In the case of a searching algorithm, the task is to **find** the location of a certain item in a list or to **verify** if the item is in the list. There are several different searching algorithms which can be used in varying circumstances. The three studied below are **linear search**, **binary search** and a **binary tree search**. **Hash tables** are not searching algorithms, but function in a similar way.

### Synoptic Link

A **hash table** is a data structure that creates a mapping between keys and values.

They are covered further in **Hash Tables** under **Fundamentals of Data Structures**.

### Synoptic Link

The ideas of time complexity, space complexity and Big-O notation are covered in **Order of Complexity** under **Theory of Computation**.

## Linear Search

A linear search can be conducted on any **unordered** list. It is the most simple to program, but it has a comparatively **high time complexity**, so is rarely used in the real world. It has one loop, and thus has a **time complexity** of  $O(N)$ . In this algorithm, **each item** in the list is compared **sequentially** to the target.

### Linear Search Example 1

Here is an array of people:

Position	0	1	2	3	4	5
Data	Dean	Angelina	Seamus	Oliver	Cho	Fred

Where is “Oliver” in the array?

The first position of the array is checked.

Position	0	1	2	3	4	5
Data	Dean	Angelina	Seamus	Oliver	Cho	Fred

“Oliver”  $\neq$  “Dean”

Check the next position in the array.



Position	0	1	2	3	4	5
Data	Dean	Angelina	Seamus	Oliver	Cho	Fred

“Oliver” ≠ “Angelina”

So check the next position in the array

Position	0	1	2	3	4	5
Data	Dean	Angelina	Seamus	Oliver	Cho	Fred

“Oliver” ≠ “Seamus”

So check the next position in the array

Position	0	1	2	3	4	5
Data	Dean	Angelina	Seamus	Oliver	Cho	Fred

“Oliver” = “Oliver”

Hence Oliver is found at position 3 in the array.

### Linear Search Example 2

Where is “Hannah” in the array?

The first position of the array is checked.

Position	0	1	2	3	4	5
Data	Dean	Angelina	Seamus	Oliver	Cho	Fred

“Hannah” ≠ “Dean”

Check the next position in the array.



Position	0	1	2	3	4	5
Data	Dean	Angelina	Seamus	Oliver	Cho	Fred

“Hannah” ≠ “Angelina”

So check the next position in the array

Position	0	1	2	3	4	5
Data	Dean	Angelina	Seamus	Oliver	Cho	Fred

“Hannah” ≠ “Seamus”

So check the next position in the array

Position	0	1	2	3	4	5
Data	Dean	Angelina	Seamus	Oliver	Cho	Fred

“Hannah” ≠ “Oliver”

So check the next position in the array

Position	0	1	2	3	4	5
Data	Dean	Angelina	Seamus	Oliver	Cho	Fred

“Hannah” ≠ “Cho”

So check the next position in the array

Position	0	1	2	3	4	5
Data	Dean	Angelina	Seamus	Oliver	Cho	Fred

“Hannah” ≠ “Fred”

Check the next position in the array. There are no more positions in the array, so Hannah is not contained in the array. When correctly programmed, a linear search algorithm should **not result in an error** when trying to locate an item not in the array.



Pseudocode for a linear search algorithm could be:

```
LinearSearch(Target, ArrayofNames)
Boolean Found
Integer Count
Found ← FALSE
Count ← 0

Do Until Found == TRUE or Count == ArrayofNames Count
  If Target == ArrayofNames(Count)
    Found ← TRUE
  Else
    Count ← Count + 1
  End If
Loop

If Found = TRUE
  Output Target found at Count
Else
  Output Target not found
End if
```

Using a For...Next loop in lieu of a Do Until loop would be bad programming practice. The For...Next loop is an example of **definite iteration**, whereas the Do Until loop is an example of **indefinite iteration**. For instance, if the target was at the beginning of the array, the Do Until loop would locate the item immediately and then exit the loop, whereas a For...Next loop would still have to search through each piece of data. This makes the Do...Until loop quicker in this scenario (although both loops are  $O(N)$  as big O notation looks at the worst case scenario).

## Synoptic Link

**Iteration** is the process of repeating a block of code multiple times.

Iteration is covered under **Programming Concepts in Fundamentals of Programming.**



## Binary Search

A binary search can be used on any **ordered** list. If the list is unordered, the data must be **sorted** by a **sorting algorithm**. A binary search works by looking at the **midpoint** of a list and determining if the target is **higher or lower** than the midpoint. The time complexity is  $O(\log N)$  because the list is **halved** each search.

### Synoptic Link

A **merge sort** or a **bubble sort** can be used to order a list.

Further detail on sorting algorithms can be found under **Sorting Algorithms** in **Fundamentals of Algorithms**.

### Binary Search Example 1

Here is an array of people:

Position	0	1	2	3	4	5	6
Data	George	Percy	William	Ronald	Charles	Fredrick	Ginevra

Where is George?

This is an unordered list, so the first step is to use a sorting algorithm. The data can be sorted into **ascending or descending** order, although each will require a slightly different code.

Position	0	1	2	3	4	5	6
Data	Charles	Fredrick	George	Ginevra	Percy	Ronald	William

The first step is to take the middle piece of data. To find the midpoint of the data, **add** the **highest position** and the **lowest position** of the array being considered, and **divide by 2**. I.e.  $0 + 6 = 6$ ,  $6/2 = 3$ . Look at position 3 of the array.

Position	0	1	2	3	4	5	6
Data	Charles	Fredrick	George	Ginevra	Percy	Ronald	William

“George” ≠ “Ginevra”



“George” < “Ginevra” because George is before Ginevra when in alphabetical order. Your programming language can **compare strings** to determine whether they are higher or lower than one another.

Hence, discard all places in the array beyond “Ginevra”.

Our new array looks like this:

Position	0	1	2
Data	Charles	Fredrick	George

To find George, we must check the middle position.  $0 + 2 = 2$ ,  $2/2 = 1$ .

Position	0	1	2
Data	Charles	Fredrick	George

“George” ≠ “Fredrick”

“George” > “Fredrick”

Hence, everything before “Fredrick” does not need to be checked.

Position	2
Data	George

There is only one element in the array.  $2 + 2 = 4$ ,  $4/2 = 2$

Position	2
Data	George

“George” = “George”

George is found at position 2 of the array.





## Binary Search Example 2

Here is an array of names:

Position	0	1	2	3	4	5
Data	Mushu	Zazu	Flounder	Pascal	Gus	Baloo

Where is “Pegasus”?

The first step is to order then with a sorting algorithm.

Position	0	1	2	3	4	5
Data	Baloo	Flounder	Gus	Mushu	Pascal	Zazu

The first step is to find the midpoint.  $0 + 5 = 5$ ,  $5/2 = 2.5$ , there is no position 2.5 in the array, so an int calculation is performed on it - this removes the decimal part. Hence, we need to check the data in position 2.

Position	0	1	2	3	4	5
Data	Baloo	Flounder	Gus	Mushu	Pascal	Zazu

“Pegasus”  $\neq$  “Gus”

“Pegasus”  $>$  “Gus”, so only positions 3, 4 and 5 will be considered from now on.

Position	3	4	5
Data	Mushu	Pascal	Zazu

To find the midpoint,  $3 + 5 = 8$ ,  $8/2 = 4$ .

Position	3	4	5
Data	Mushu	Pascal	Zazu

“Pegasus”  $\neq$  “Pascal”





“Pegasus” > “Pascal”

Positions 3 and 4 are disregarded.

Position	5
Data	Zazu

There is only one piece of data in the array.  $5 + 5 = 10$ ,  $10/2 = 5$

Position	5
Data	Zazu

“Pegasus” ≠ “Zazu”

“Pegasus” > “Zazu”

There is no more data to check; Pegasus isn't in the array.



A binary search can be conducted in many different ways. Here is pseudocode for one solution:

```
BinarySearch(Target, ArrayofNames)
  Integer TopPointer
  Integer BottomPointer
  Integer Midpoint
  Boolean Found

  Found ← FALSE
  BottomPointer ← 0
  TopPointer ← ArrayofNames Count - 1

  Do Until Found = TRUE or TopPointer < BottomPointer
    Midpoint = int mid TopPointer, BottomPointer
    If ArrayofNames(Midpoint) = Target
      Found = TRUE
    ElseIf ArrayofNames(Midpoint) > Target
      TopPointer = Midpoint - 1
    ElseIf ArrayofNames(Midpoint) < Target
      BottomPointer = Midpoint + 1
    End If
  Loop

  If Found = TRUE
    Output Target found at Midpoint
  Else
    Output Target not found
  End if
```

A binary search can also be completed through **recursion**.

### Synoptic Link

**Recursion** refers to a block of code calling itself in order to complete a task.

Recursion is covered in **recursive techniques in fundamentals of programming**.



## Binary Tree Search

A binary tree search is the same as a binary search, except it is conducted on a **binary tree**. A tree is an **acyclic, connected graph**, and a binary tree is a **rooted ordered tree** in which **each node has 0, 1 or 2 children**. Like a binary search, a binary tree search has a time complexity of  $O(\log N)$ .

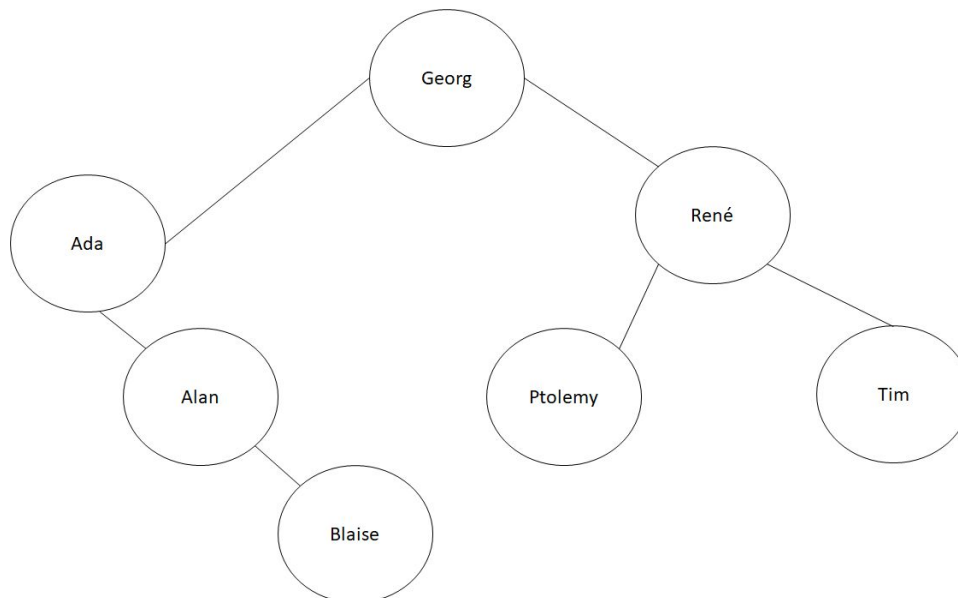
### Binary Tree Search Example

Here is a list of names:

Georg, René, Ada, Alan, Blaise, Ptolemy, Tim.

Does the list contain “Alan”?

The first stage in a binary tree search is to put the list into a **binary tree**.



A binary tree search starts at the root.

### Synoptic Link

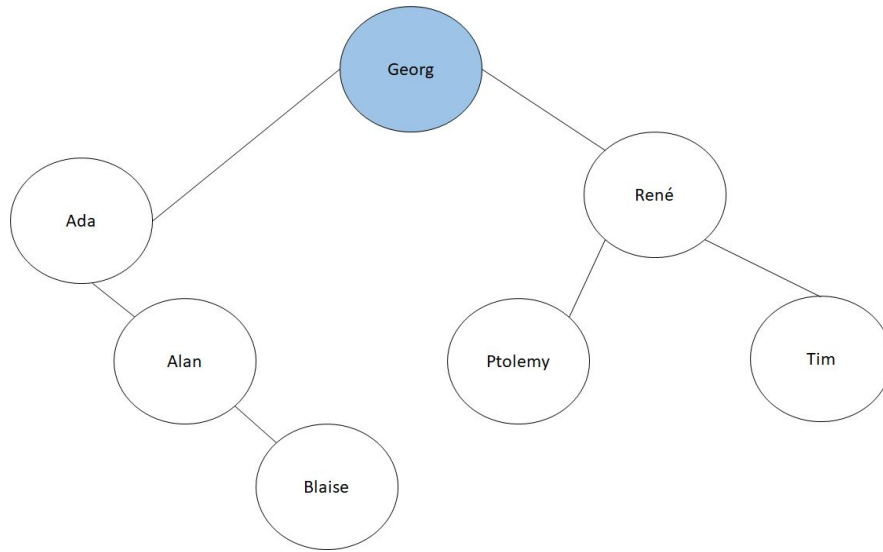
**Graphs** can be used as **visual representations of complex relationships**.

Graphs are covered in **Graphs** under **Fundamentals of Data Structures**.

### Synoptic Link

Information on how to create **binary trees** can be found under **Trees** in **Fundamentals of Data Structures**.

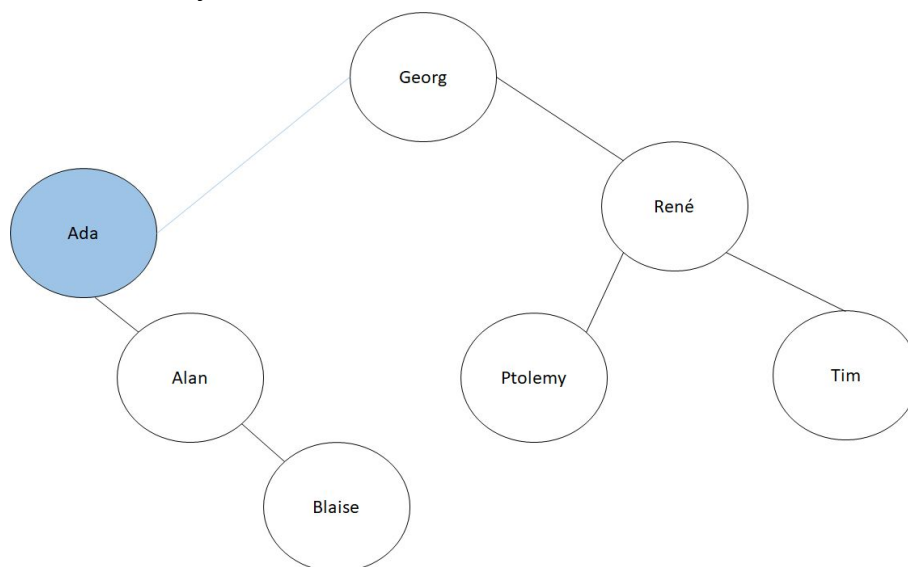




“Alan” ≠ “Georg”

“Alan” < “Georg”

Therefore only items **left** of the root will be considered further.

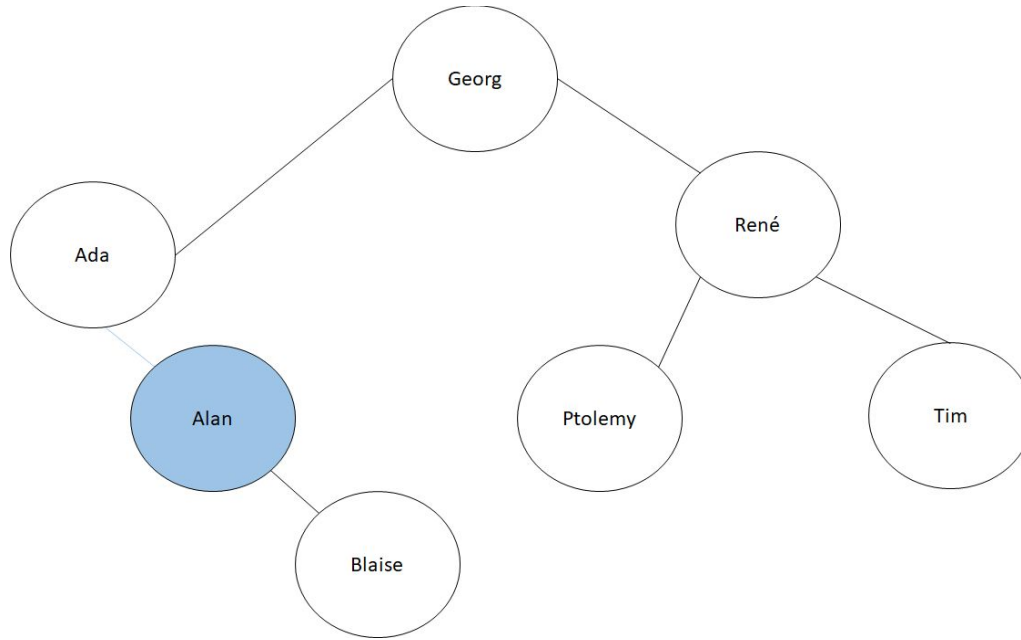


“Alan” ≠ “Ada”

“Alan” > “Ada”

Hence only nodes **right** of Ada will be further considered.





“Alan” = “Alan”  
Alan is in the tree.

